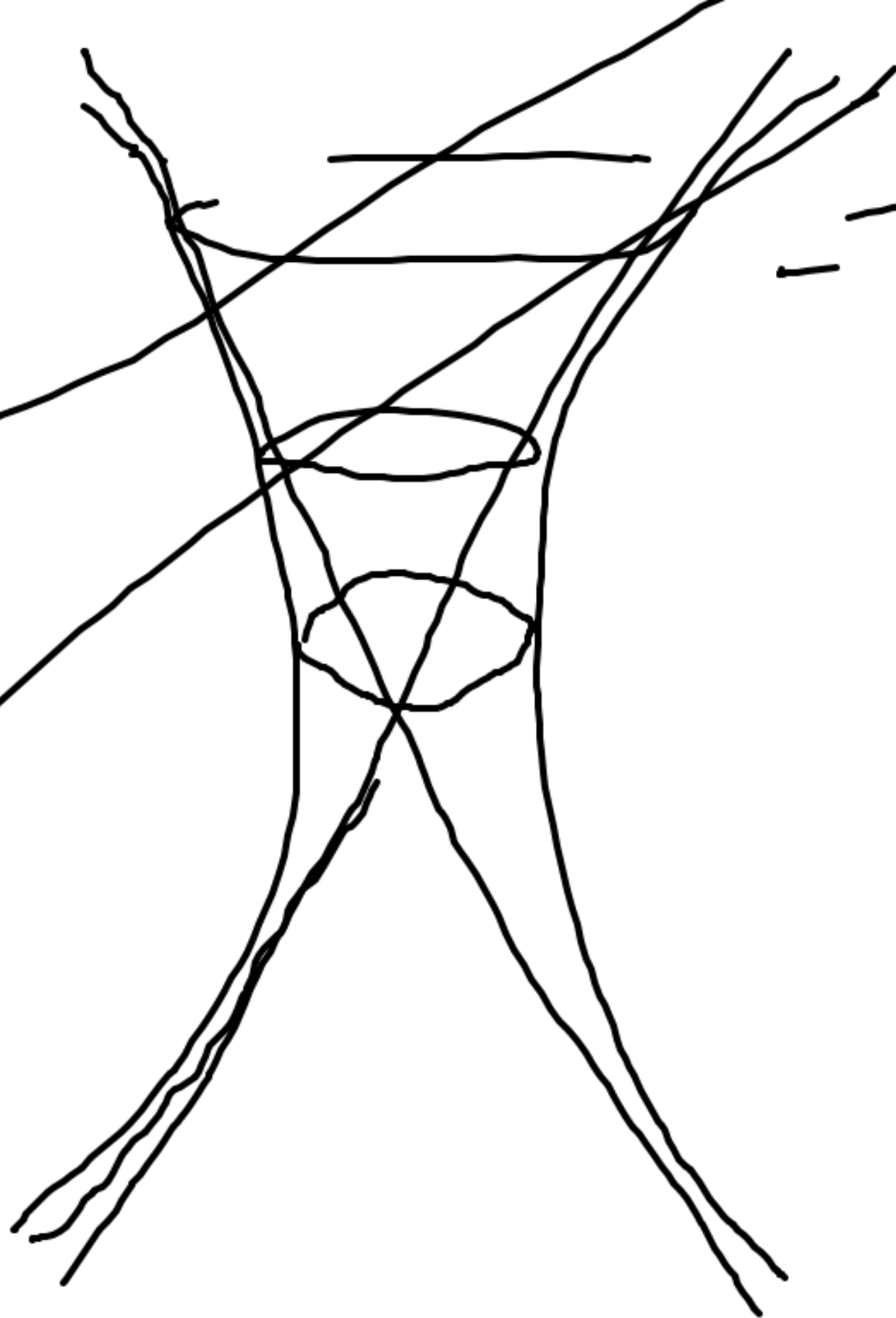


$T - W$
 $= \text{const}$

$$-T^2 + W^2 + X^2 + Y^2 + Z^2 = T^2$$



$$H^2 = -\frac{K}{a^2} + \underbrace{\frac{8\pi}{3} \rho}$$

$$P = \alpha \rho \quad \frac{8\pi}{3} \frac{\rho_i}{a^3(1 \pm \epsilon)}$$

$$\phi \rightarrow S = \frac{1}{2} \underbrace{\int_V \sqrt{g}}_{\text{Volume}} g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi - m^2 \phi^2$$

$$\sqrt{g} = a^3$$

$$d^3x dt$$

$$\frac{1}{a^3} \partial_t a^3 \partial_t \phi + m^2 \phi = 0$$

if we assume hsm.

ϕ .

$$\partial_t^2 \phi + \underbrace{3H \partial_t \phi}_{\text{}} + m^2 \phi = 0$$

For large H , neglect $(\partial_t^2 \phi)$

$$\partial_t \phi = -\frac{m^2}{H} \phi \quad \partial_t^2 \phi \approx \left(\frac{m^2}{H}\right)^2 \phi$$

$m^2/H \ll 1$ Slow Roll

$$H = \frac{8\pi}{3} \rho$$

$$T_{\mu\nu} = \partial_\mu \phi \partial_\nu \phi - \frac{1}{2} \left(\partial_\alpha \phi \partial^\alpha \phi + m^2 \phi^2 \right) g_{\mu\nu}$$

$$P = -\rho = -m^2 \phi^2 \Rightarrow \rho = \frac{P}{\alpha}$$

$$\rho = \frac{P}{\alpha}$$

Not quite

ϕ rolls down hill
eventually $(\partial\phi)^2$ dominates.

ϕ begins to move faster
than H ($\frac{\dot{\phi}}{\phi} > H$)

$$\frac{m^2}{H^2} \ll 1.$$

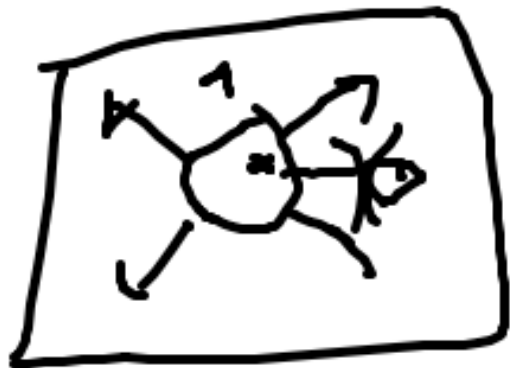
$$H^2 = \frac{8\pi}{3}$$

$$\rho = \frac{8\pi}{3} m^2 \phi^2$$

$$\text{If } \underline{\phi \gg 1}$$

Puzzles : Hom. + Isot r.

$$\underline{m^2 \phi^2} \rightarrow V(\phi)$$



LINDE - Slow Roll.
Inflation

$$\frac{1}{a^2} \partial_r \partial_r \psi_k + \frac{k^2}{a^2} \psi_k = 0$$

e^{ikx} If $H^2 > \frac{k^2}{a^2}$
 Then ψ_k roughly const.

$\lambda_{ph} > \frac{1}{H}$ then ψ does not
 change much.

$$\int a^3 (\partial_t \Phi)^2 - a (\partial_x \Psi)^2$$

$$H_K = \int \frac{\pi^2}{a^3} + k^2 a \Psi^2$$

$\Downarrow$

$\Delta \pi \quad \Delta \Psi \Rightarrow h = 1$

$$H_K = \frac{\cancel{\Delta \pi}^2}{a^3 \Delta \Psi^2} + k^2 a \Delta \Psi^2 = E_K$$

$\Delta \Psi^2 = \frac{1}{k a^2}$

$\Delta\psi$ becomes much larger
than ψ minimum.

$\downarrow E_K$ becomes $\gg \hbar\omega$.

$\Delta\pi \rightarrow$ small.

Squeezed State.

As universe expands

+ the H grows.

— This excess energy fluctu-
ates - seeds for
galaxy growth.

Scale invariant fluctuations.

$\Rightarrow$ CMB structure.



Cepheid. + S.N 1^a

$$\Rightarrow H \sim 74 \text{ km/sec/Mpc}$$

$$\text{CMB} \quad \sim 67 \text{ "/s/Mpc}$$

$$\pm 2 \text{ km/s/Mpc}$$

5 σ discrepancy.

New Physics?