Physics 200-05 Mini Test Solutions

The class average (out of 1 max for each question) is listed at the beginning of the question.

1. [.4] Given two matrices,

$$A = \begin{pmatrix} 2 & 0 \\ 1 & 1 \end{pmatrix} \tag{1}$$

$$B = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \tag{2}$$

a) What is AB?

$$AB = \begin{pmatrix} 2 & 0 \\ 1 & -1 \end{pmatrix}$$

b) What is the determinant of B?

2. [.66] Given the complex numbers

$$x = 1 + 2i \tag{3}$$

$$y = 3i \tag{4}$$

 $\frac{\text{What is } xy}{-6+3i}$

3. [.23] A particle of mass 1Kg and velocity 1 m/s travelling in the x direction collides with another particle of mass 2 kg and speed 0 m/s. What is the final velocity of the two particles assuming that the collision is elastic and the velocities after the collision are all purely in the x direction?

1 Kg mass at -1/3 m/s, 2 Kg mass at 2/3 m/s

4. [.15] What is the taylor series expansion to second order in x of the function

$$f(x) = \sqrt{1 - x} \tag{5}$$

around the point x=0?

$$1-x/2-x^2/8+O(x^3)$$

5. [.4] What is the solution of the differential equation

$$\frac{dy(x)}{dx} = 5y(x) \tag{6}$$

assuming that the value of y(0)=1.

$$y(x) = e^{5x}$$

6) [.13] What is the kinetic energy, the potential energy, and the total energy of a particle of mass m in circular orbit around a star of mass M, at a distance R away from the central star? (the mass m may be assumed to be very much $\frac{\text{smaller than } M.)}{\text{Balance of angular acceleration vs gravitational force}}$ $\frac{mv^2}{R} = \frac{GMm}{R^2}$ Thus

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$$KE = \frac{1}{2}mv^2 = \frac{GMm}{2R}$$

$$PE = -\frac{GMm}{R}$$

Thus $KE = \frac{1}{2}mv^2 = \frac{GMm}{2R}$ $PE = -\frac{GMm}{R}$ $Total = -\frac{GMm}{2R}$ The above assumes that M is stationary, and that the smaller particle orbits around that stationary location of M.